Tunable Electronic Properties of Two-Dimensional Transition Metal Dichalcogenide Alloys: A First-Principles Prediction

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ABSTRACT: We investigated the composition-dependent electronic properties of two-dimensional transition-metal dichalcogenide alloys (W$_x$Mo$_{1-x}$S$_2$) based on first-principles calculations by applying the supercell method and effective band structure approximation. It was found that hole effective mass decreases linearly with increasing W composition, and electron effective mass of alloys is always larger than that of their binary constituents. The different behaviors of electrons and holes in alloys are attributed to the fact that metal d-orbitals have different contributions to conduction bands of MoS$_2$ and WS$_2$ but almost identical contributions to valence bands. We examined the conduction polarity of W$_x$Mo$_{1-x}$S$_2$ monolayer alloys with four metal electrode materials (Au, Ag, Cu, and Pd). It suggests the main carrier type for transport in transistors could change from electrons to holes as W composition increases if high work function metal contacts were used. The tunable electronic properties of two-dimensional transition-metal dichalcogenide alloys make them attractive for electronic and optoelectronic applications.

Recent progress, challenges, and opportunities in two-dimensional (2D) materials beyond graphene have been reviewed. Single-layered transition-metal dichalcogenides (TMDs) as a novel class of 2D materials have caught our attention. The versatile chemistry and unique electrical and optical properties of TMDs make them attractive for a variety of applications ranging from hydrogen evolution, energy storage, to transistors, photodetectors, and electroluminescent devices. Bulk TMDs are van der Waals solids with a layered structure similar to graphite: within each layer, a plane of metal atoms is sandwiched between, and covalently bonded to two planes of chalcogen atoms. They can be exfoliated mechanically or chemically into mono- or few-layered TMDs. Synthesis of large-area ultrathin MoS$_2$ layers using chemical vapor deposition (CVD) has also been demonstrated. Interestingly, TMDs such as MoS$_2$ and WS$_2$ exhibit a transition from an indirect bandgap semiconductor in the bulk to a direct bandgap semiconductor in the monolayer, which has been manifested by enhanced photoluminescence in the monolayer as well as theoretical band structure calculations. In contrast to the semimetallic graphene sheet, the MoS$_2$ monolayer has a sizable bandgap (~1.8 eV) and field-effect transistors (FETs) made of it show high room-temperature current on/off ratios (>10$^5$). It exhibits n-type conductivity with an electron effective mass ~0.48m$_0$ and room-temperature mobility >200 cm$^2$V$^{-1}$s$^{-1}$ in top-gated transistors with a high-dielectric gate, benefited from screening of impurity scatterings by the dielectric engineering. Also, first-principles calculations predicted a room-temperature electron mobility of 130−420 cm$^2$V$^{-1}$s$^{-1}$, and the charge transport behavior in it was found to be dominated by optical phonon scatterings via intra- and intervalley scattering mechanism and Fröhlich interaction.

With carrier mobility comparable to Si, 2D semiconducting TMDs have been suggested for flexible and transparent electronic applications.

The unique properties of semiconducting TMD monolayers can be extended by alloying two compounds of different electronic properties. The transition metal atomic mixing in W$_x$Mo$_{1-x}$S$_2$ single layers has been visualized and quantified recently. We have shown in an earlier study that bandgaps of atomically thin TMD alloys are tunable by mixing MoS$_2$ and WS$_2$ and controlling the composition of alloys. TMD monolayer alloys have opened new possibilities for band structure engineering and electronic and optoelectronic applications. The fundamental electronic properties of these 2D alloys form the physical basis for the fabrication of FET devices based on them and provide guidance for the selection of metal electrode materials. Both theoretical predictions of electronic properties and device characterization of charge transport behaviors have been performed for pure and single-layered TMDs. Among these, MoS$_2$ is most extensively studied. However, investigations on the electronic properties of 2D...
TMD alloys are still lacking. In this Letter, we focus on the composition-dependent electronic properties of 2D alloys \( W_x Mo_{1-x} S_2 \) and report tunable effective masses of charge carriers and conduction polarity in 2D TMD alloys \( W_x Mo_{1-x} S_2 \) based on first-principles predictions.

The electronic structures of \( W_x Mo_{1-x} S_2 \) monolayer alloys were determined first-principly by applying the supercell method and the effective band structure (EBS) approximation.\(^{23}\) Although disordered alloys \( A_1 \cdots B_2 \cdots C \) constructed by ordered constituents \( A \) and \( B \) are inevitably associated with loss of long-range order, and then automatic loss of the concept of band structure \( E(\mathbf{k}) \), the language of effective band structure continues to be enormously useful for phenomenologically describing and discussing electronic properties of random alloys. The EBS approximation maps the eigenvalues obtained from large supercell calculations into an effective band structure in the primitive cell, and is able to recover an approximate \( E(\mathbf{k}) \) for alloys. The experimental observables for alloys are very often interpreted in terms of such quantities as approximate exchange-correlation functional of local density approximation (LDA)\(^{24}\) and the projector augmented wave (PAW) \(^{25,26}\) within a 9х9 supercell of \( W_x Mo_{1-x} S_2 \) monolayer alloys in the \( x\cdots y \) and \( x\cdots z \) planes, respectively.

To obtain the EBS of random alloys, we need to transform eigenstates in the large supercell into an effective band structure in the primitive cell. This unfolding procedure can be described by a spectral function (SF) of the continuous energy variable \( E \):

\[
A(\mathbf{k}, E) = \sum_{mn} |\langle \mathbf{k}|n\rangle|^2 \delta(E_m - E) \tag{1}
\]

where \( |\mathbf{k}m\rangle \) and \( |\mathbf{k}m\rangle \) (\( n \) and \( m \) are band indices) are the Bloch states in the primitive cell and supercell, respectively. With the SF determined for a set of \( |\mathbf{k}\rangle \) (a given \( |\mathbf{k}\rangle \) is mapped precisely into a single \( |\mathbf{k}\rangle \) according to the geometry and symmetry of the supercell and its primitive cell) and over a wide range of energies, we subsequently constructed the EBS of random alloys. For the supercell of ordered systems, SF is a set of \( \delta \)-functions because the symmetry does not change when going from the primitive cell to the supercell. However, for alloys, the symmetry is broken, and different local environments in the alloys are reflected by a finite width of SF defined in eq 1. The detailed description about the EBS method can be found in ref 23.

The energy \( E(\mathbf{k}) \) at which the SF shows a peak value and closest to the band edge was chosen for the parabolic fitting to obtain the effective mass. Also, for the parabolic fitting along each direction, we chose five \( E(\mathbf{k}) \) with \( |\mathbf{k}| \) in the vicinity of the K-point. The EBS along high symmetry lines for a random configuration of \( W_{0.5} Mo_{0.5} S_2 \) monolayer alloys is plotted in Figure 2. It can be seen that the conduction band (CB) has a broader SF than the valence band (VB) (see the light-blue shaded areas of Figure 2), which reflects different influences of local environments on the CB and VB of the alloys. The EBS of alloys also shows that \( W_{0.5} Mo_{0.5} S_2 \) monolayer alloys are direct band gap semiconductors, with band edges of CB and VB coinciding at the K-point. However, the energy difference between the K- and Y-point (located in the midway between \( \Gamma-\)
Figure 2. Effective band structure of one of configurations of W$_{0.5}$Mo$_{0.5}$S$_2$ alloys. It is a direct band gap ($E_{\text{gap}} = 1.78$ eV). The different k vectors in the primitive cell are represented by a thin vertical line. The red areas represent the spectral functions $A(k, E)$ at each k point, and the blue shaded areas represent the width of $A(k, E)$ for CB and VB. The inset displays the first Brillouin zone of the primitive cell with three high symmetry points Γ, K, and M, as well as a special Y-point along the Γ−K direction.

Figure 3. Composition-dependent effective masses of electrons and holes for W$_{x}$Mo$_{1-x}$S$_2$ monolayer alloys. The blue square represents the effective mass of electrons, while the red circle represents that of holes. The error bars represent the standard deviation of electron (hole) effective masses calculated for eight random configurations. $m_0$ is the bare electron mass.

effective masses of W$_{x}$Mo$_{1-x}$S$_2$ have a negative effect on electron transport; (iv) in contrast to the electron effective mass, the hole effective mass decreases linearly with increasing W composition, and the error bars are small, indicating little influence of metal configurations on the hole effective mass; (v) the hole effective mass is always smaller than the electron effective mass in W$_{x}$Mo$_{1-x}$S$_2$ monolayer alloys for all W compositions x (except for x = 0 and 1).

To understand these results, we examined the absolute energy level (Table S5 of the SI), the composition (Figure 4), and charge density distribution (Figure S1 of the SI) of the frontier orbitals in MoS$_2$, W$_{0.5}$Mo$_{0.5}$S$_2$, and WS$_2$ respectively. The absolute energy levels of HOMO and LUMO in MoS$_2$ and WS$_2$ were determined by the method of vacuum level calibration. To obtain the vacuum level, we recalculated the band energies of MoS$_2$ and WS$_2$ with an interlayer distance of 30 Å (see Figure S2 and eq S1 in the SI for more details). It is found that the HOMO and LUMO levels of WS$_2$ are both higher than those of MoS$_2$, which is easy to understand because W is heavier than Mo. The projected density-of-states (PDOS) analysis for the frontier orbitals were provided in Figure 4 and Table S5 of the SI. As seen, the metal contribution to HOMO is $d_{xy}$ and $d_{2z^2}$ orbitals for both MoS$_2$ and WS$_2$; by contrast, the metal contribution to LUMO is $d_{x^2}$ orbitals for MoS$_2$, but $d_{xy}$, $d_{2z^2}$, and $d_{xy}$ orbitals for WS$_2$. Based on the frontier orbital analysis, we explain different behaviors of electrons and holes in W$_{x}$Mo$_{1-x}$S$_2$ monolayer alloys as follows: (i) W atoms directly participate in the formation of HOMO in alloys due to identical orbital compositions for MoS$_2$ and WS$_2$. Meanwhile, the electronic coupling in WS$_2$ is stronger than that in MoS$_2$, so that the hole effective mass of WS$_2$ is smaller. These two facts together lead to a linear decrease of the hole effective mass with increasing W composition; (ii) due to different compositions of LUMO for MoS$_2$ and WS$_2$, and lower LUMO level of MoS$_2$, mixing of W atoms into MoS$_2$ only slightly reduces the electronic coupling and increases the electron effective mass.

On the other side, mixing of Mo atoms into WS$_2$ leads to a sudden increase in the electron effective mass because the electronic properties of LUMO of alloys is mainly determined by Mo atoms due to the lower LUMO level of MoS$_2$. From the above analysis, it is clear that 2D W$_{x}$Mo$_{1-x}$S$_2$ alloys always have a larger electron effective mass than either MoS$_2$ or WS$_2$, and alloying could not improve the electron mobility in n-type...
transistors. The hole effective mass decreases linearly as the W composition increases, so the hole mobility is likely to be enhanced.

In FETs, the main carrier type for transport is to a large extent decided by the relative position of the metal work function (WF) of source/drain electrodes and the energy level of frontier orbitals of semiconductors in the channel. The transistor usually exhibits n-type conduction if the LUMO level of semiconductor is closer to the Fermi level of metal electrode (the Fermi level $E_F = -WF$); otherwise it exhibits p-type conduction. Here we examined four common metal electrode materials (Au, WF = 5.2 eV; Ag, WF = 4.2 eV; Cu, WF = 4.6 eV; Pd, WF = 5.12 eV), and compared their Fermi levels with the frontier orbital levels of $W_{x}Mo_{1-x}S_2$ with different W compositions. The absolute levels of HOMO and LUMO in $W_{x}Mo_{1-x}S_2$ monolayer alloys were determined by the method of vacuum level calibration as described above, and they were plotted as a function of W compositions in Figure 5 along with the Fermi levels of Au, Ag, Cu and Pd. We see that the HOMO level rises linearly as W atoms in the alloys increase; instead, the LUMO level exhibits an energy bowing as a function of W composition. So the bandgap bowing effect in $W_{x}Mo_{1-x}S_2$ monolayer alloys originates from the bowing of LUMO level. The energy level shift of HOMO and LUMO with increasing W composition is in line with the effective mass change of holes and electrons demonstrated above. The results shown in Figure 5 tell us that (i) for Ag and Cu electrodes, the LUMO level of $W_{x}Mo_{1-x}S_2$ alloys is located closer to the Fermi level of electrodes and therefore more conducive to electron injection, so the main carrier type should always be electrons in this case no matter what the W composition is; (ii) for Au and Pd electrodes, when the W composition is low, the LUMO level is closer to the Fermi level of Au and Pd, and the $W_{x}Mo_{1-x}S_2$ monolayer exhibits an n-type conductivity; when $x$ is above ~0.13 the main carrier type changes from electrons to holes.

| Table 1. The Electron (Hole) Effective Mass (in $m_0$) along the K−Γ (m$_{K−Γ}$) and K−M (m$_{K−M}$) Directions as well as the Geometric Mean $m^{*}_{eff} = (m^{*}_{K−Γ}m^{*}_{K−M})^{1/2}$ for $W_{x}Mo_{1−x}S_2$. |
|-----------------|-------|-------|-------|-------|-------|-------|-------|-------|
| $x$      | 0.0   | 0.158 | 0.356 | 0.687 | 0.918 | 1.0   |
| $m_{K−Γ}^{*}$ | 0.537 | 0.65 (0.06) | 0.70 (0.04) | 0.62 (0.05) | 0.59 (0.06) | 0.55 (0.06) | 0.52 (0.08) | 0.49 (0.09) | 0.47 (0.11) | 0.45 (0.09) | 0.43 (0.07) | 0.42 (0.06) |
| $m_{K−M}^{*}$ | 0.591 | 0.62 (0.03) | 0.58 (0.03) | 0.54 (0.03) | 0.51 (0.03) | 0.48 (0.03) | 0.45 (0.03) | 0.43 (0.03) | 0.41 (0.03) | 0.39 (0.03) | 0.37 (0.03) | 0.35 (0.03) |
| $m_{K−Γ}$ | 0.61 (0.12) | 0.60 (0.10) | 0.58 (0.09) | 0.56 (0.09) | 0.54 (0.09) | 0.52 (0.09) | 0.50 (0.09) | 0.48 (0.10) | 0.46 (0.11) | 0.44 (0.10) | 0.42 (0.09) | 0.40 (0.08) |
| $m_{K−M}$ | 0.65 (0.08) | 0.70 (0.06) | 0.75 (0.05) | 0.80 (0.06) | 0.85 (0.07) | 0.90 (0.08) | 0.95 (0.09) | 1.00 (0.10) | 1.05 (0.11) | 1.10 (0.10) | 1.15 (0.10) | 1.20 (0.10) |
| $m^{*}_{eff}$ | 0.60 (0.04) | 0.63 (0.04) | 0.66 (0.04) | 0.69 (0.05) | 0.72 (0.05) | 0.75 (0.06) | 0.78 (0.06) | 0.81 (0.07) | 0.84 (0.08) | 0.87 (0.09) | 0.90 (0.09) | 0.93 (0.10) |

Figure 4. Projected density-of-states for the valence and conduction bands of MoS$_2$, W$_{0.5}Mo_{0.5}S_2$, and WS$_2$, respectively. The 9 × 9 supercell was used for the calculations and analysis. It is noted that the composition of the valence bands of MoS$_2$ and WS$_2$ is almost identical at the band edge, and d-electrons of Mo and W have equal contributions to the valence band edge of W$_{0.5}Mo_{0.5}S_2$. The composition of the conduction bands of MoS$_2$ and WS$_2$ is quite different at the band edge, and d-electrons of Mo have major contributions to the conduction band of W$_{0.5}Mo_{0.5}S_2$. A quantified analysis of PDOS is provided in Table S5 of the SI.
levels of frontier orbitals in 2D TMDs can be tuned by alloying, metal electrodes, and at certain compositions ambipolar transport is possible. In combination with our electrodes, and at certain compositions ambipolar transport is likely to change from n-type to p-type in FETs with high work function metal contacts such as Ti resulted in ambipolar behavior at low temperature. 41 Recent, high-performance single layered WSe2 p-FETs with chemically doped contacts have been reported. 42 A high hole mobility of ~250 cm² V⁻¹ s⁻¹ and current on/off ratio of >10⁶ at room temperature were achieved by lowering the contact resistance for hole injection using high work function Pd contacts and degenerate surface doping of the contacts by patterned NO2 chemisorption on WSe2. By contrast, lower work function metal contacts such as Ti resulted in ambipolar transport behavior with low current levels owing to high Schottky barrier heights to both CB and VB of WSe2. A systematic selection of the contact metal toward the design of high-performance n-type monolayer WSe2 FETs has been demonstrated. 43 It was found that In electrode, among others (Ti, Ag, and Al), leads to small ohmic contact resistance with WSe2 and an electron mobility of 142 cm² V⁻¹ s⁻¹ at room temperature. These experiments demonstrate how the conduction polarity in FETs changes with the selection of metal electrode materials. We show that the absolute energy levels of frontier orbitals in 2D TMDs can be tuned by alloying, and the conduction polarity of alloys is tunable.

Above all, we have demonstrated that both the effective mass and the conduction polarity are tunable by mixing MoS2 and WS2, but due to identical contributions of metal d-electrons to the HOMO whereas different contributions of metal d-electrons to the LUMO for MoS2 and WS2, mixing W into MoS2 benefits the hole transport instead of the electron transport. Other 2D TMD alloys have also been theoretically studied, for example, the stability of MoSe2, Se+1 monolayer alloys was discussed recently. Such alloys are predicted to be thermodynamically stable and to be manufactured using CVD or exfoliated from the bulk mixed materials. 44,45 One of works also predicted tunable bandgaps in the mixed compounds, but detailed analysis of electronic properties were not conducted. Our preliminary calculations show that MoSe2 and MoSe2 have almost identical compositions for both HOMO and LUMO, and the effective masses of electrons and holes of MoSe2 are both slightly larger than those of MoS2. It seems to suggest that mixing in the chalcogen sublattice is a less effective way in engineering the electronic properties of TMDs than mixing in the metal sublattice, because the metal d-electrons have more significant contributions to the frontier orbitals of alloys than the chalcogen p-electrons.

Finally, we present a brief discussion of the stability of 2D W,Mo1−xS2 alloys with different W compositions. The free energy and internal energy of mixing per primitive cell for the alloys were calculated following the work of Komsa et al. 46 and plotted as a function of W composition at 300 K (Figure S3 of the SI). In our calculations the experimental lattice constant of 2H-MoS2 was used for all compositions of the alloys, but the general trend of the free energies and internal energies is consistent with that of Komsa et al.: the internal energies of mixing are negative for all random configurations, and the free energies of mixing are more negative than the corresponding internal energies due to the favorable entropy change of mixing. These results demonstrated that W,Mo1−xS2 monolayers are thermodynamically stable. In most cases, the formation energy of semiconductor alloys is positive due to the large lattice mismatch between the constituents. Here, the lattice constants of MoS2 and WS2 are very close (~0.2%), and we expect the the strain energy in their alloys is negligible. In our calculations, the negative internal mixing energy is only due to the charge exchange. According to the Madelung energy model, the sign of charge exchange enthalpy for a ternary alloy depends on the additional charge exchange. 47,48 Our internal mixing energy is only ~4 meV, which indicates that the charge exchange in the alloys is small. Overall, the formation of W,Mo1−xS2 alloys can be attributed to the tiny lattice mismatch and the additional charge exchange. In fact, 2D W,Mo1−xS2 alloys have been successfully manufactured through exfoliation from the bulk mixed materials recently. 49

To summarize, we have investigated the electronic properties of 2D W,Mo1−xS2 alloys with different W compositions x based on first-principles calculations. The free energies of mixing are negative for these monolayer alloys, indicating that they are thermodynamically stable at the room temperature. Interestingly, the hole effective mass of alloys decreases linearly with increasing W composition, and the electron effective mass is always larger than that of MoS2 or WS2 monolayer, due to (i) almost identical orbital compositions of HOMO for MoS2 and WS2 and very different orbital compositions of LUMO; (ii) both HOMO and LUMO levels of MoS2 are lower than those of WS2. This finding suggests that mixing of W atoms into MoS2 does not favor the electron conduction, and it could
enhance the hole mobility instead. In addition, the main carrier type for transport in FETs could change from electrons to holes with increasing W composition in the alloys due to that the high WF of Au and Pd in the source and drain electrodes is closer to the lifted HOMO level of the alloys. Combining these two findings, we conclude that 2D alloys of MoS2/WxS2 exhibit better p-type conductivity than MoS2 and at certain alloy compositions ambipolar behavior is likely to show up. The tunable electronic properties of 2D TMD alloys could open new opportunities for them to be used in electronic and optoelectronic devices.

**ASSOCIATED CONTENT**

Supporting Information
SOC and convergence tests; electron (hole) effective mass for WxMo1−xS monolayer alloys at eight random configurations and with different W compositions; absolute energy levels, PDOS analysis, and charge density distribution of HOMO and LUMO for MoS2, W0.5Mo0.5S2, and WS2; internal energies and free energies of mixing for WxMo1−xS monolayer alloys at different W compositions. This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes
The authors declare no competing financial interest.

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